

Interference on thin film

Lecture 6

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The reflected light from surface AB and CD ultimately meet at point O . The intensity at point O depends on the path difference between the two light rays.

If n be the refractive index of the film then path difference

$$l = n (QN_1 + N_1 R + RS) - QN \quad \dots\dots\dots(1)$$

From the geometry $RS=RM$ and $SL =LM= d$ (d thickness of the film at point S)

Now from Snell's law $n = \sin i / \sin r = \frac{QN/QS}{QN_1/QS}$

$$QN = n \cdot QN_1$$

Putting the value of QN in equation 1 we get

$$\begin{aligned} l &= n (N_1R + RS) \\ &= n (N_1R + RM) = n \cdot N_1M \\ &= n \cdot 2d \cos(r-\alpha) \quad \dots\dots\dots(2) \end{aligned}$$

Since the light ray suffering reflection from the surface 1 backed by denser medium it suffers a phase difference π and corresponding path difference $\lambda/2$ hence total path difference between the two interfering wave is

$$l = 2nd \cos (r-\alpha) + \lambda/2$$

Conditions for maxima and minima:

We know that the condition for **bright fringe** at O

$$2nd \cos (r-\alpha) + \lambda/2 = \text{even multiple of } \lambda/2$$

$$2nd \cos (r-\alpha) = \text{odd multiple of } \lambda/2 = (2m + 1)\lambda/2$$

where $m = 0, 1, 2, 3, \dots$

Similarly for **dark fringe**

$$2nd \cos (r-\alpha) = \text{even multiple of } \lambda/2$$

$$= (2m)\lambda/2$$

Note that for a parallel film $\alpha = 0$

Fringes with monochromatic light :

Since n , r , α , λ are constants so order no of bright and dark fringe only depend on the value of d . Where d is practically zero, the path difference between the two rays is $\lambda/2$. Hence we get dark fringe there.

If the film is extremely thin then $d=0$ for the whole film, then the film surface will be perfectly dark even for white light also.

If $\alpha =0$, then for oblique incidence film surface will be dark bright and dark according as the value of angle r . If a parallel beam incident normally on the film, then the whole surface will be bright or dark depending upon the value of d .

Fringes with white light :

For parallel beam of white light the value of n, λ, r are different for different colours . Where d is practically zero we get dark fringe for all colours for the path difference $\lambda/2$. Since λ for violet light is smaller than the red light the first order bright fringe will be formed at a smaller thickness than the red colour. Thus we get coloured fringes at different thickness.
