

# Interference on thin film

## Lecture 6

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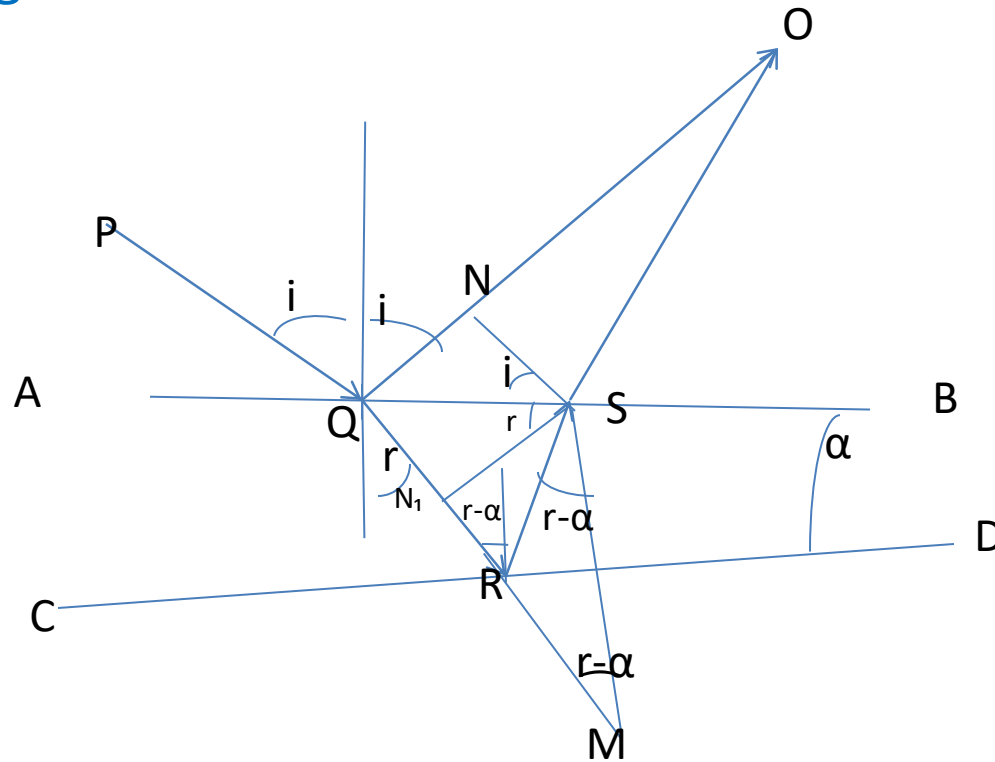
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Interference on thin film (for reflected system):

ABCD is a wedge shaped film enclosing an angle  $\alpha$ . PQ is a monochromatic light of wave length  $\lambda$ .  $i$  is the angle of incident and  $r$  angle of refraction inside the thin film .  $r-\alpha$  is the angle of incidence for the 2<sup>nd</sup> surface.



The reflected light from surface AB and CD ultimately meet at point O . The intensity at point O depends on the path difference between the two light rays.

If  $n$  be the refractive index of the film then path difference

$$l = n ( QN_1 + N_1 R + RS) - QN \quad \dots\dots\dots(1)$$

From the geometry  $RS=RM$  and  $SL =LM= d$  (  $d$  thickness of the film at point S)

Now from Snell's law  $n = \sin i / \sin r = \frac{QN/QS}{QN_1/QS}$

$$QN = n \cdot QN_1$$

Putting the value of  $QN$  in equation 1 we get

$$\begin{aligned} l &= n ( N_1R + RS) \\ &= n ( N_1R + RM) = n \cdot N_1M \\ &= n \cdot 2d \cos(r-\alpha) \quad \dots\dots\dots(2) \end{aligned}$$

Since the light ray suffering reflection from the surface 1 backed by denser medium it suffers a phase difference  $\pi$  and corresponding path difference  $\lambda/2$  hence total path difference between the two interfering wave is

$$l = 2nd \cos (r-\alpha) + \lambda/2$$

### Conditions for maxima and minima:

We know that the condition for **bright fringe** at O

$$2nd \cos (r-\alpha) + \lambda/2 = \text{even multiple of } \lambda/2$$

$$2nd \cos (r-\alpha) = \text{odd multiple of } \lambda/2 = (2m + 1)\lambda/2$$

where  $m = 0, 1, 2, 3, \dots$

Similarly for **dark fringe**

$$2nd \cos (r-\alpha) = \text{even multiple of } \lambda/2$$

$$= (2m)\lambda/2$$

Note that for a parallel film  $\alpha = 0$

## **Fringes with monochromatic light :**

Since  $n$ ,  $r$ ,  $\alpha$ ,  $\lambda$  are constants so order no of bright and dark fringe only depend on the value of  $d$ . Where  $d$  is practically zero, the path difference between the two rays is  $\lambda/2$ . Hence we get dark fringe there.

If the film is extremely thin then  $d=0$  for the whole film, then the film surface will be perfectly dark even for white light also.

If  $\alpha =0$ , then for oblique incidence film surface will be dark bright and dark according as the value of angle  $r$ . If a parallel beam incident normally on the film, then the whole surface will be bright or dark depending upon the value of  $d$ .

## **Fringes with white light :**

For parallel beam of white light the value of  $n, \lambda, r$  are different for different colours . Where  $d$  is practically zero we get dark fringe for all colours for the path difference  $\lambda/2$ . Since  $\lambda$  for violet light is smaller than the red light the first order bright fringe will be formed at a smaller thickness than the red colour. Thus we get coloured fringes at different thickness.

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